

**Treat the following exercises:**

**I. Fill in the following truth table:**

(3 pts)

A	B	A	B	A.B	$\overline{A+B}$	A.B	$A.B.(A+B)+A.B$
0	0						
0	1						
1	0						
1	1						

**II. Using exclusively the Boolean algebra, demonstrate that :**

(3 pts)

- $(A + B)(A + \overline{B}) = A$
- $AB + \overline{B}C + \overline{A}C = AB + \overline{A}C$
- $AB + \overline{A}B = AB + \overline{A}B$

**III. Give the simplified functions of the following tables using the Karnaugh map :**

(3 pts)

	$\overline{C}\overline{D}$	$\overline{C}D$	$CD$	$C\overline{D}$
AB	0	0	1	0
AB	1	1	1	1
AB	1	1	1	1
AB	0	1	0	0

Table 1

	$\overline{C}\overline{D}$	$\overline{C}D$	$CD$	$C\overline{D}$
AB	0	1	1	0
AB	1	1	1	1
AB	0	1	1	0
AB	0	1	1	0

Table2

	$\overline{C}\overline{D}$	$\overline{C}D$	$CD$	$C\overline{D}$
AB	0	0	0	0
AB	1	1	1	1
AB	0	0	0	0
AB	1	1	1	1

Table 3

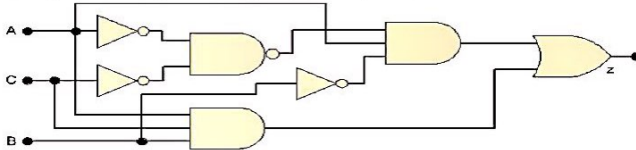
**IV. Realize a logic circuit with 3 inputs (A, B, C) and 2 outputs (F<sub>0</sub>, F<sub>1</sub>) and which gives the number of 1s applied at the inputs:**

(4 pts)

- Build the corresponding truth table.
- Find the logical expression of the output F<sub>0</sub>.
- Find the logical expression of the output F<sub>1</sub>.
- Simplify the expression of F<sub>0</sub>.
- Draw the simplified circuit of F<sub>0</sub> with NAND gates two-input only.

**V. What is the logical function performed by the following circuit?**

(2½ pts)



**VI. Fill in the table below for a multiplexer of 4-inputs (I<sub>3</sub>, I<sub>2</sub>, I<sub>1</sub>, I<sub>0</sub>), two selections inputs (S<sub>1</sub>, S<sub>0</sub>) and one output:**

(2 pts)

I <sub>3</sub>	I <sub>2</sub>	I <sub>1</sub>	I <sub>0</sub>	S <sub>1</sub>	S <sub>0</sub>	Output
1	1	1	1			
0	1	0	0			
1	1	0	1			
1	1	1	0			

**VII. Complete the following table:**

(2 ½ pts)

X	Y	Z	CK	Q <sub>A</sub>	Q <sub>B</sub>	F
1	0	1	↑			
0	1	0				
1	1	1				
0	0	1				
1	1	1				
0	0	0				
0	1	1				
1	1	1				

Knowing that:

- X and Y are respectively the values of J and K of a JK flip-flop named A.
- Y and Z are respectively the values of J and K of a JK flip-flop named B.
- $F = Q_A \oplus Q_B$ .

I-	A	B	$\bar{A}$	$\bar{B}$	A.B	$\overline{A+B}$	$\bar{A}\bar{B}$	A.B( $\overline{A+B}$ ) $\bar{A}\bar{B}$
	0	0	1	1	0	0	1	1
	0	1	1	0	0	1	0	0
	1	0	0	1	0	0	0	0
	1	1	0	0	1	0	0	1

II a)  $(A+B)(A+\bar{B}) = A$   
 $AA + A\bar{B} + AB + B\bar{B} = A$   
 $A + A\bar{B} + AB = A$   
 $A(1 + \bar{B} + B) = A$   
 $A = A \checkmark$

b)  $AB + \underbrace{BC}_{\text{consensus Term}} + \bar{A}C = AB + \bar{A}C$   
 $AB + (A+\bar{A})(BC) + \bar{A}C = AB + \bar{A}C \checkmark$   
 $AB + ABC + \bar{A}BC + \bar{A}C = AB + \bar{A}C$   
 $AB(1+C) + \bar{A}C(B+1) = AB + \bar{A}C$   
 $AB + \bar{A}C = AB + \bar{A}C$

c)  $\bar{A}\bar{B} + \bar{A}B = \bar{A}(\bar{B} + B) = \bar{A}$   
 $(\bar{A} + B)(A + \bar{B}) = \bar{A}B + \bar{A}\bar{B}$   
 $\bar{A}A + \bar{A}\bar{B} + AB + B\bar{B} = \bar{A}\bar{B} + AB$   
 $\bar{A}\bar{B} + AB = \bar{A}\bar{B} + AB$

III -

	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	0	0	1	0
$\bar{A}B$	1	1	1	1
$A\bar{B}$	1	1	1	1
$AB$	0	1	0	0

Table 1  
 $B + A\bar{C}\bar{D} + \bar{A}C\bar{D}$

	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	0	1	2	0
$\bar{A}B$	1	1	1	1
$A\bar{B}$	0	1	1	0
$AB$	0	1	1	0

Table 2  
 $D + \bar{A}\bar{B}$

	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	0	0	0	0
$\bar{A}B$	1	1	1	1
$A\bar{B}$	0	0	0	0
$AB$	1	1	1	2

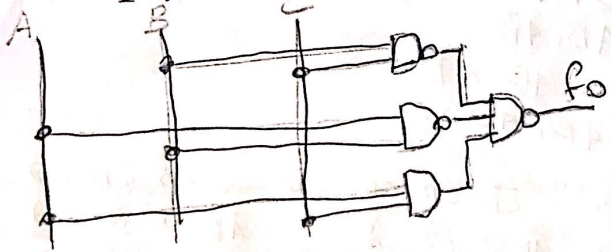
Table 3  
 $\bar{A}\bar{B} + \bar{A}B$

IV-a)

	A	B	C	f <sub>0</sub>	f <sub>1</sub>
0	0	0	0	0	0
0	0	1	0	1	1
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	1	1
1	0	1	1	0	0
1	1	0	1	0	0
1	1	1	1	1	1

b)  $f_0 = \bar{A}BC + A\bar{B}C + AB\bar{C} + ABC$   
 c)  $f_1 = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + ABC$   
 d)  $f_0 = \bar{A}BC + A\bar{B}C + AB\bar{C} + ABC$   
 $= B(\bar{A} + A) + A\bar{B}C + ABC$   
 $= BC + A\bar{B}C + ABC$   
 $= C(B + AB) + A\bar{B}C$   
 $= C(B + A) + A\bar{B}C$   
 $= BC + AC + A\bar{B}C$   
 $= B(C + AC) + AC$   
 $= B(C + A) + AC$   
 $= BC + AB + AC$

e)  $f_0 = BC + AB + AC$   
 $= \overline{\bar{B}\bar{C}} = \overline{AB} = \overline{AC}$



V.  $Z = (\bar{A}\bar{C} \cdot A \cdot \bar{B}) + AB$

VI.

I <sub>3</sub>	I <sub>2</sub>	I <sub>1</sub>	I <sub>0</sub>	S <sub>1</sub>	S <sub>0</sub>	output
1	1	1	1	1	0	I <sub>2</sub>
0	1	0	0	0	1	I <sub>1</sub>
1	1	0	1	1	1	I <sub>3</sub>
1	1	1	0	0	0	I <sub>0</sub>

VII-

X	Y	Z	C.K.	$\bar{A}$	$\bar{B}$	F
1	0	1		1	0	1
0	1	0		0	1	1
1	1	1		1	0	1
0	0	1		1	0	1
1	1	1		0	1	1
0	0	0		0	1	1
0	1	1		0	0	0
1	1	1		1	1	0

$$F = A \oplus B = A\bar{B} + \bar{A}B$$

0 *सत्य*  
1 *जुलिया*